

## Chapter 5 - Sneak Peek

**I CAN....**

- Multiply polynomials
- Determine the domain & range of a function
- Solve an exponential function using logarithms
- Rewrite a logarithm in exponential form.
- Factor polynomials
- Find the inverse of a function
- Rewrite an exponential equation as a logarithm

1. Multiply each of the following. Be sure to show all your work.

1a.  $(x+1)(x-5)$

$x^2 - 4x - 5$

1b.  $(6x + 3)(x^2 + 5x - 9)$

$$\begin{array}{r} x^2 \quad 5x \quad -9 \\ 6x \quad | \quad 6x^3 \quad 30x^2 \quad -54x \\ 3 \quad | \quad 3x^2 \quad 15x \quad -27 \end{array}$$

$6x^3 + 33x^2 - 39x - 27$

1c.  $(x - 3)^2(2x - 7)$

$$(x-3)(x-3)(2x-7)$$

$$(x^2 - 6x + 9)(2x-7)$$

$$\begin{array}{r} x^2 \quad -6x \quad 9 \\ 2x \quad | \quad 2x^3 \quad -12x^2 \quad 18x \\ -7 \quad | \quad -7x^2 \quad 42x \quad -63 \end{array}$$

$2x^3 - 19x^2 + 60x - 63$

2. Factor the expressions.

2a.  $4y^2 - 49$

$(2y-7)(2y+7)$

2b.  $y^2 - 13y + 42$

~~$\begin{array}{r} 42 \\ -6 \times 7 \\ -13 \end{array}$~~

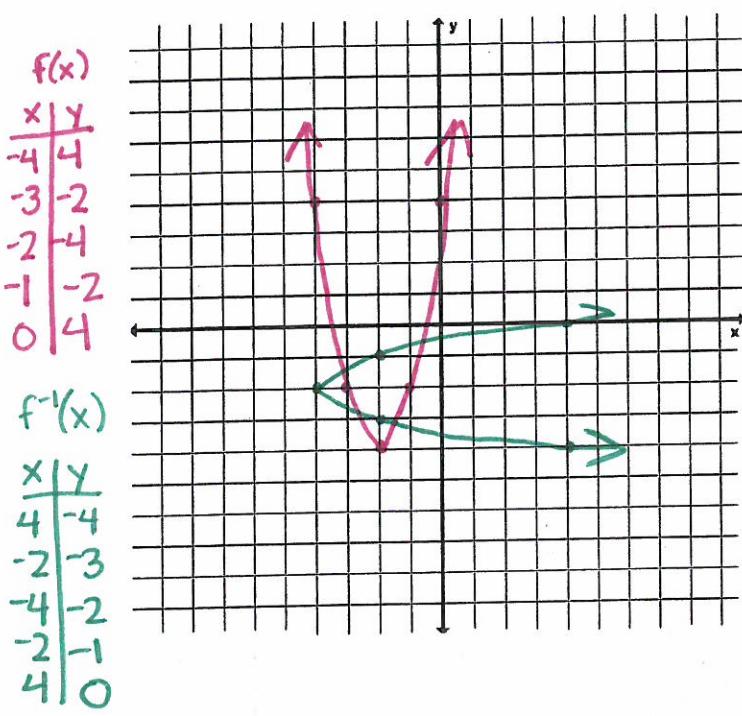
$(y-6)(y-7)$

2c.  $6y^2 - 7y - 10$

$$\begin{array}{r} y \quad -2 \\ 6y \quad | \quad 6y^2 \quad -12y \\ 5 \quad | \quad 5y \quad + 10 \end{array}$$
 ~~$\begin{array}{r} -60 \\ -12 \times 5 \\ -7 \end{array}$~~

$(6y+5)(y-2)$

3. Graph  $f(x) = 2(x + 2)^2 - 4$  AND its inverse on the graph below.



Is the inverse a function?

No

Why or why not?

bc it doesn't pass the Vertical Line Test

State the domain and range of each graph.

$$f(x) = 2(x + 2)^2 - 4$$

$$\text{Domain: } (-\infty, \infty)$$

$$\text{Range: } [-4, \infty)$$

Inverse Graph

$$\text{Domain: } [-4, \infty)$$

$$\text{Range: } (-\infty, \infty)$$

4. Find the inverse of each of the following functions

4a.  $g(x) = -7x - 1$

$$\begin{array}{rcl} x & = & -7y - 1 \\ & +1 & +1 \\ \hline x+1 & = & -7y \end{array}$$

$$\begin{array}{rcl} \frac{x+1}{-7} & = & y \\ \hline \end{array}$$

$$\frac{x+1}{-7} = g^{-1}(x)$$

or

$$g^{-1}(x) = -\frac{x+1}{7}$$

4b.  $g(x) = 9(x + 7)^2$

$$\begin{array}{rcl} x & = & 9(y+7)^2 \\ \hline \frac{x}{9} & = & (y+7)^2 \end{array}$$

$$\frac{x}{9} = (y+7)^2$$

$$\sqrt{\frac{x}{9}} = y+7$$

$$\begin{array}{rcl} \frac{\sqrt{x}}{3} - 7 & = & y \\ \hline \end{array}$$

4c.

$$f(x) = \frac{\sqrt[3]{7+x}}{9} - 7$$

$$x = \frac{\sqrt[3]{7+y}}{9} - 7$$

$$x+7 = \frac{\sqrt[3]{7+y}}{9}$$

$$9(x+7) = \sqrt[3]{7+y}$$

$$[9(x+7)]^3 = 7+y$$

$$f^{-1}(x) = [9(x+7)]^3 - 7$$

$$\begin{matrix} \\ \\ \end{matrix}$$

4d.

$$f(x) = \frac{\sqrt{x+5}}{2} - 3$$

$$x = \frac{\sqrt{y+5}}{2} - 3$$

$$x+3 = \frac{\sqrt{y+5}}{2}$$

$$2(x+3) = \sqrt{y+5}$$

$$(2(x+3))^2 = y+5$$

$$f^{-1}(x) = [2(x+3)]^2 - 5$$

5. Without using your calculator, simplify each expression. make sure your answer contains only positive exponents. You must show step by step work in order to earn full credit.

5a.

$$(2x^3y^{-5})^{-2}$$

$$2^{-2}x^{-6}y^{10}$$

$$\frac{y^{10}}{2^2x^6} = \frac{y^{10}}{4x^6}$$

5b.

$$\frac{xy^7}{x^5} \cdot \frac{x^3y^9}{x^2y^{11}}$$

$$\frac{x^4y^{16}}{x^7y^{11}}$$

$$\frac{y^5}{x^3}$$

5c.

$$(4x^{-4}y^3)^{-3} \cdot (5x^6y)^2$$

$$4^{-3}x^{12}y^{-9} \cdot 5^2x^{12}y^2$$

$$\frac{5^2x^{12}x^{12}y^2}{4^3y^9}$$

$$\frac{25x^{24}}{64y^7}$$

5d.

$$(4x^{-2}y^{-1})^4$$

$$4^4x^{-8}y^{-4}$$

$$\frac{256}{x^8y^4}$$

5e.

$$\frac{x^5y^2}{x^{-2}} \cdot \frac{x^7y^{-1}}{x^9y^3}$$

$$\frac{x^{12}y^1}{x^7y^3}$$

$$= \frac{x^5}{y^2}$$

5f.

$$(x^{-6}y^5)^{-1} \cdot (7x^2y^6)^0$$

$$x^6y^{-5} \cdot 1$$

$$\frac{x^6}{y^5}$$

6a. Determine the missing value for the question mark.

$$\log_5 125 = ?$$

$$5^? = 125$$

$$? = \boxed{3}$$

6b.

$$\log_7 2401 = ?$$

$$7^? = 2401$$

$$? = \boxed{4}$$

6c.  $\log_? 121 = 2$

$$?^2 = 121$$

$$? = \boxed{11}$$

6d.

$$\log_? 64 = 3$$

$$?^3 = 64$$

$$? = \boxed{4}$$

6e. Rewrite each of the following exponential equations as logarithms.

$$2^4 = 16$$

Log Form:

$$\log_2 16 = 4$$

6f.

$$6^7 = 279936$$

Log Form:

$$\log_6 279936 = 7$$

6g. Rewrite each of the following logarithmic equations as an exponential equation.

$$\log_5 x = \frac{1}{6}$$

Exponential Form:

$$5^{\frac{1}{6}} = x$$

6h.

$$\log_2 x = \frac{1}{4}$$

Exponential Form:

$$2^{\frac{1}{4}} = x$$

6i. Solve the following equations.  
(using logarithms may be useful)

$$8^x = 43$$

$$\log_8 43 = x$$

$$x \approx 1.8088$$

6j.

$$27^x = 101$$

$$\log_{27} 101 = x$$

$$x \approx 1.4003$$